Design and Control of a CSTR for Production of Ethyl Acetate

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Abstract
Ethyl acetate is produced by the reaction of ethanol and acetic acid in presence of sulphuric acid as a catalyst. The reaction is exothermic and the temperature of the reaction should be controlled at the desired value for optimum conditions. The level of the reactants and composition of the product should also be tightly controlled. A cascade control is used to control both the reaction and the jacket temperatures, so the rise in temperature will not affect the quality of the product. A control strategy was developed, the transfer functions were specified and use for simulation for each loop and selection of a controller that gives the best performance.

Keywords: Control Strategy, Design and Simulation, CSTR, Tuning, Control Loop, Cascade Control, Transfer Functions.

I. Introduction
Feedback control is the simplest type of control system for automatic process control that compensates for the process upsets. However, the disadvantage of feedback is that it only reacts after the process has been upset. Thus, a deviation on the controlled variable is needed to initiate corrective action. Cascade control is control system that in some applications significantly improves the performance provided by the feedback control. Cascade control is implemented in order to improve the disturbance rejection properties of the controlled system. The introduction and use of an additional sensor that allows for a separation of the fast and slow dynamics of the process results in a nested loop configuration, each loop has associated its corresponding controller. The fast dynamics of the inner loop will provide faster disturbance attenuation and minimize the possible effect of disturbance before they affect the primary output. This set up involves two controllers, it is therefore needed to tune both PID controllers. The usual approach involves the tuning of the secondary controller while setting the primary controller in manual mode. On a second step, the primary controller is tuned by considering the secondary controller acting on the inner loop. It is therefore a more complicated design procedure than that of a standard single-loop based PID control system.[4]

II. Martials and Methods
Cascade Control
The system under consideration is an ideal CSTR with an exothermic reversible reaction; the liquid phase esterification of ethyl alcohol with acetic acid in the presence of sulphuric acid as a catalyst:

\[ C_2H_5OH + CH_3COOH \rightarrow CH_3COOCH_2H_5 + H_2O \]

The dynamic of this process is highly non-linear mainly due to the heat generation process. Many reactors are inherently unstable, so an effective and well-designed control system is necessary in order to assure stable operation. The instability appears when reversible exothermic reactions are carried out in a CSTR. These reactions tend to produce a large increment in temperature, forcing the rupture of safety and reducing the life time of the reactor. The faster reaction goes, the more heat is generated, heating up the reaction mass, and consequently, raising the reactor temperature and increasing the rate of reaction. So under these conditions, the system can reach undesirable high temperature state. The solution to this problem is a temperature control system capable of detecting the rising of the reactor
temperature is affected by changes in disturbance variables such as reactant feed temperature or feed composition. The simple feedback control strategy would handle such disturbance by adjusting a control valve on the cooling water inlet.

However, an increase in the inlet cooling water temperature, an unmeasured disturbance, can cause unsatisfactory performance. The resulting increase in the reactor temperature, due to a reduction in heat removal rate, may occur slowly. If appreciable dynamic lags occur in the jacket as well as in the reactor, the corrective action taken by the controller could be delayed. To avoid this disadvantage, a feedback controller for the jacket temperature, whose set point is determined by the reactor temperature controller, can be added to provide cascade control. The control system measures the jacket temperature, compare it to a set point, and adjusts the cooling water makeup. The reactor temperature set point and both measurements are used to adjust a single manipulated variable, the cooling water make up rate. The principal advantage of the cascade control strategy is that a second measured variable is located close to a potential disturbance and its associated feedback loop can react quickly. Thus, improving the closed-loop response.

A control strategy was developed, transfer functions have been identified and we control the temperature inside the reactor and jacket temperature by cascade loop as show in figure(1), and control the concentration of reactant (feed stream), also control the level inside the reactor. All loops had to be analyzed for stability and Tuning. By Routh - Hurwitz, Root Locus, Direct substitution, and Bode methods.

Figure 1: Control Strategy of CSTR reactor for Ethyl Acetate production
Identification of Transfer Functions of Control Loops

From the literature [3] the following transfer functions are obtained:

**Loop1:**

\[ G_C = K_C \]

\[ G_P = \frac{1}{(s+1)(4s+1)} \] \hspace{2cm} \text{(1)}

\[ G_V = \frac{2.5}{0.2s^2+1.5s+1} \] \hspace{2cm} \text{(2)}

\[ G_m = 1.0 \]

**Loop2:**

\[ G_C = K_C \]

\[ G_P = \frac{1}{2s+1} \] \hspace{2cm} \text{(3)}

\[ G_V = \frac{3.5}{2.5s^2+1.5s+1} \] \hspace{2cm} \text{(4)}

\[ G_m = \frac{1.5}{0.2s+1} \] \hspace{2cm} \text{(5)}

**Cascade Control Loops**

\[ G_{cI} = K_{cI} \] \hspace{2cm} \text{(6)}

\[ G_{cII} = K_{cII} \] \hspace{2cm} \text{(7)}

\[ G_{pI} = \frac{12.8}{16.7s+1} \] \hspace{2cm} \text{(8)}

\[ G_{pII} = \frac{1.8+1}{0.9175+1} \] \hspace{2cm} \text{(9)}

\[ G_v = \frac{6.6}{0.95+1} \] \hspace{2cm} \text{(10)}

\[ G_{mII} = \frac{1}{2s+1} \] \hspace{2cm} \text{(11)}

\[ G_{mI} = 1.0 \] \hspace{2cm} \text{(12)}
Loop 1:

\[ 1 + \text{OLTF} = \frac{(0.2s^2 + 1.5s + 1)(s+1)(4s+1) + 2.5KC}{(0.2s^2 + 1.5s + 1)(s+1)(4s+1)} \]  \hspace{1cm} (13)

The characteristic equation is \(1 + \text{OLTF} = 0\)

The Characteristic equation of loop 1 is:

\[(0.2s^2 + 1.5s + 1)(s+1)(4s+1) + 2.5KC \]  \hspace{1cm} (14)

\[0.8s^4 + 7s^3 + 11.7s^2 + 6.5s + 1 + 2.5KC = 0\]  \hspace{1cm} (15)

Figure 2: Block diagram of loop 1
Root Locus for Loop 1:

![Root Locus for Loop 1](image1)

Figure 3: Root Locus for Loop 1

The Bode Plot Method:

![Bode Plot for Loop 1](image2)

Figure 4: Bode Plot for Loop 1

### Table 1: Values of Ultimate Gain (Ku) and Ultimate Period (Pu) for Loop 1

<table>
<thead>
<tr>
<th>Method</th>
<th>Ku</th>
<th>Pu (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Routh - Hurwitz</td>
<td>3.67</td>
<td>5.86</td>
</tr>
<tr>
<td>Root Locus</td>
<td>30.8</td>
<td>1.898</td>
</tr>
<tr>
<td>Bode</td>
<td>27.19</td>
<td>1.98</td>
</tr>
</tbody>
</table>
Loop 2

\[ K_C \rightarrow \frac{3.5}{2.5S^2 + 1.5S + 1} \rightarrow \frac{1}{(2s + 1)} \rightarrow R(S) \]

\[ \frac{1.5}{0.2s + 1} \]

Tuning of loop 2:

\[ 1 + \text{OLTF} = \frac{(2.5s^2 + 1.5s + 1)(2s + 1)(0.2s + 1) + 5.25KC}{(2.5s^2 + 1.5s + 1)(2s + 1)(0.2s + 1)} \]  \hspace{1cm} (16)

Root Locus Method:

Figure 6: Block diagram for loop 2

Figure 7: Root Locus for Loop 2

Figure 8: Bode plot for Loop 2
**Table 2: Values of Ultimate Gain (Ku) and Ultimate Period (Pu) for Loop 2**

<table>
<thead>
<tr>
<th>Method</th>
<th>Ku</th>
<th>Pu (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Routh - Hurwitz</td>
<td>2.07</td>
<td>3.63</td>
</tr>
<tr>
<td>Root Locus</td>
<td>12.7</td>
<td>2.47</td>
</tr>
<tr>
<td>Bode</td>
<td>4.88</td>
<td>6.799</td>
</tr>
</tbody>
</table>

**Figure 9: Step Response for Loop 2**

**Cascade control**

![Cascade Control Diagram]

\[ 1+\text{OLTF} = \frac{(0.95+1)(0.9175+1)(2s+1)+12.15K_{clII}}{(0.95+1)(0.9175+1)(2s+1)} \]

\[ \text{..........................(17)} \]
Outer Loop (Primary Loop):

The Characteristic equation of outer loop (primary loop)

\[ 1 + \frac{G_d G_c I G_p I I G_v}{1 + G_d G_i G_p I I} = 0 \]  \hspace{1cm} (18)
Figure 14: Step Response for Primary Loop

Root Locus Method:

Table 4: Values of Ultimate Gain (\(K_u\)) and Ultimate Period (\(P_u\)) for Primary Loop

<table>
<thead>
<tr>
<th>Method</th>
<th>(K_u)</th>
<th>(P_u) (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Routh - Hurwitz</td>
<td>0.320</td>
<td>5.555</td>
</tr>
<tr>
<td>Root Locus</td>
<td>0.304</td>
<td>6.662</td>
</tr>
<tr>
<td>Bode</td>
<td>1.565</td>
<td>6.425</td>
</tr>
</tbody>
</table>

Figure 15: Root Locus for Primary Loop

The Bode Plot Method:

Figure 16: Bode Plot for Primary Loop
Table 5: Average Values of Ultimate Gain (Ku) and Ultimate Period (Pu) for Loops 1 to 4

<table>
<thead>
<tr>
<th>Loop</th>
<th>Ku (av)</th>
<th>Pu (av) sec</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loop1</td>
<td>20.55</td>
<td>3.246</td>
</tr>
<tr>
<td>Loop2</td>
<td>6.55</td>
<td>4.299</td>
</tr>
<tr>
<td>Loop3</td>
<td>0.769</td>
<td>4.857</td>
</tr>
<tr>
<td>Loop4</td>
<td>0.534</td>
<td>6.214</td>
</tr>
</tbody>
</table>

Table 6: Using Ziegler – Nichols’ method to tuning parameters by using Ku (average) and Pu (average)

<table>
<thead>
<tr>
<th>Type of Controller</th>
<th>Kc</th>
<th>τI (sec)</th>
<th>τD (sec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>P</td>
<td>3.55</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>PI</td>
<td>3.195</td>
<td>3.88</td>
<td>-</td>
</tr>
<tr>
<td>PID</td>
<td>4.26</td>
<td>2.33</td>
<td>0.58</td>
</tr>
</tbody>
</table>

III. Conclusion and Recommendation

From this study it’s proved that Routh array, Root locus and Bode method give almost equal ultimate gains and ultimate periods therefor, the average was taken for the loop simulation. It is concluded that any method of the can be selected and use confidently for tuning and stability analysis. Further work is recommended to be carried out to transfer the control system to digital ad SCADA systems.

References